CALCULATION POLICY



Fritchley C.E. Aided Primary School



Progression towards a standard written method of calculation INTRODUCTION

This calculation policy has been written in line with the programmes of study taken from the revised National Curriculum for Mathematics (2014). It provides guidance on appropriate calculation methods and progression. The content is set out in yearly blocks under the following headings: addition, subtraction, multiplication and division.

Statements taken directly from the programmes of study are listed in bold at the beginning of each section.

Children will use mental methods as their first port of call when appropriate, but for calculations that they cannot do in their heads, they will need to use an efficient written method accurately and with confidence.

AIMS OF THE POLICY

- To ensure consistency and progression in our approach to calculation
- To ensure that children develop an efficient, reliable, formal written method of calculation for all operations
- To ensure that children can use these methods accurately with confidence and understanding

HOW TO USE THIS POLICY

- If, at any time, children are making significant errors, return to the previous stage in calculation
- Always use suitable resources, models and images to support children's understanding of calculation and place value, as appropriate
- Encourage children to make sensible choices about the methods they use when solving problems

N.B. Examples in this policy are to show how we do calculations at different stages. All Year Groups should be following 'Rising Stars' teaching sequences.

Stages in Addition

Addition – Stage 1

Children will engage in a wide variety of songs and rhymes, games and activities. They will begin to relate addition to combining two groups of objects, first by counting all and then by counting on from the largest number.

They will find one more than a given number.

In practical activities and through discussion they will begin to use the vocabulary involved in addition.





'You have five apples and I have three apples. How many apples altogether?'

Addition – Stage 2

- Given a number, identify one more
- Read, write and interpret mathematical statements involving addition (+) and the equals (=) sign
- Add one- digit and two-digit numbers within 20, including zero
- Solve missing number problems eg 10 + = 16

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Children will continue to practise counting on from any number e.g. 'Put five in your head and count on four.'

Initially use a number track to count on for addition, counting on from the largest number:



'Put your finger on number six and count on six.'



Ensure children are confident with using a marked number line before moving on to an empty number line (see stage 3 guidance).

Continue to practise counting on from the largest number for addition with totals within 20.

Addition – Stage 3

- Add numbers using concrete objects, pictorial representations, and mentally, including:
 - A two digit number and ones
 - A two digit number and tens
 - Two two-digit numbers
 - Three one-digit numbers

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Counting on in ones using an empty number line, within 100...

28 + 6 = 34



Use in conjunction with a 100 square to show jumps of tens.

48 + 36 = 84

'Put the biggest number first (48), and then partition the smaller number (36 = 30 + 6) and count on: 48 + 30 + 6.'



Use in conjunction with a 100 square to show jumps of tens and ones.

If children are confident, use more efficient jumps...



Use in conjunction with a 100 square to show jumps of tens and ones/units.

Also use the partitioning method to add two two-digit numbers:

$$43 + 25 = 68$$

$$40 \ 3 \ 20 \ 5$$

$$40 + 20 = 60$$

$$3 + 5 = 8$$

$$60 + 8 = 68$$

'Partition the numbers into tens and ones.

Add the tens together and then add the ones together. Recombine to give the answer'.

Then move on to calculations that **bridge** the tens:

$$48 + 36 = 40 + 8 + 30 + 6$$
$$40 + 30 = 70$$
$$8 + 6 = 14$$
$$70 + 14 = 84$$

This is an alternative way of recording the partitioning method.

Further develop addition with numbers that bridge 100, using a **200 grid** to support.

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Addition – Stage 4

• Add numbers with up to three digits, using formal written method of columnar addition

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Further develop the use of the empty number line with calculations that bridge 100:



The partitioning method can also be used with three-digit numbers.

Introduce the **expanded written method** with the calculation presented both horizontally and vertically (in columns).

Initially use calculations where it has not been necessary to bridge across the tens or hundreds:

```
63 + 32 = 95
 60 and 3
                                        'Partition the numbers into tens and ones. Add the
+ 30 and 2
                                        tens together and then add the ones together.
 90 and 5 = 95
                                               Recombine to give the answer.'
Then...
      63
    + 32
                                  Add the least significant digits (ones) together first and then
        5 (ones)
                                  the tens in preparation for the formal written method.
                                  Writing the units and tens is not necessary as long as the
      90 (tens)
                                  children understand the method.
      95
```

This will lead into the formal written method...

63

00	
+32	Use the language of place value to ensure understanding:
95	'Three add two equals five. Write five in the ones column.
	60 add 30 equals 90. Write 9 (90) in the tens column.

NB Informal/mental methods would be more appropriate for numbers of this size, but use two-digit numbers when introducing the columnar method.

Then introduce calculations where it is necessary to bridge:

68+ 24Add the least significant digits (ones) together first and then the
tens in preparation for the formal written method.12 (ones)Writing the units and tens is not necessary as long as the
children understand the method.

If children are ready, introduce the formal written method, where it is necessary to 'carry' ten from the ones to the tens column:

	Use the language of place value to ensure understanding:
	'Eight add four equals 12. Write two in the ones column and
68	'carry' one (10) across into the tens column. 60 add 20 and the
<u>+ 24</u>	ten we 'carried' equals 90. Write 9 (90) in the tens column.
_ <u>92</u>	92 is the answer.'
1	

The digit that has been 'carried' should be recorded under the line in the correct column.

When **children are confident**, extend with examples where it is necessary to bridge across the tens and the hundreds:

76 + 47 = 123

76	Add the least significant digits (ones) together first and then the
<u>+ 47</u>	tens in preparation for the formal written method.
13 (ones)	Writing the ones and tens is not necessary as long as the
<u>110 (tens)</u>	children understand the method.
123	

If children are ready introduce the formal written method, where it is necessary to 'carry' across the columns and bridge 100:

76 + 47 = 123	Use the language of place value to ensure understanding:
	Seven add six equals 13. Write 3 in the ones column and 'carry'
47	one (10) across to the tens column. 40 + 70 and the ten that we
<u>+ 76</u>	'carried' equals 120. Write 2 (20) in the tens column and 'carry'
123	one (100) across into the hundreds column (100).
11	

The digits that have been 'carried' should be recorded under the line in the correct column.

If **children are confident**, further develop with the addition of a three- digit number and a two - digit number:

178 + 43 = 221

178 <u>+ 43</u> <u>221</u> 1 1

N.B. If, at any time, children are making significant errors, return to previous stage in calculation.

Addition – Stage 5

• Add numbers with up to 4 digits using the formal written method of columnar addition where appropriate

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to teach the use of **empty number lines** with three and four digit numbers, as appropriate.

Further develop the formal written method of addition, with three-digit numbers. Revisit the **expanded method** first, if necessary:

<u>н. . а . і</u>

176 + 147 = 323

176	
<u>+ 147</u>	
13	(ones)
110	(tens)
+ 200	(hundreds)
323	

Writing the ones and tens is not necessary as long as the children understand the method.

This will lead into the formal written method...

176 + 147 = 323

Use the language of place value to ensure understanding:
Seven add six equals 13. Write 3 in the ones column and
'carry' one across into the tens column (10). 40 add 70 and then
the ten that we carried equals 120. Write 2 in the tens column
(20) and 'carry' 1 (100) across into the hundreds column. 100
add 100 and the 100 that has been carried equals 300. Write 3 in the hundreds column (300)

The digits that have been 'carried' should be recorded under the line in the correct column.

If children are confident, introduce the addition of a four-digit number and a three digit number:

1845 + 526 = 2371

1	8	4	5
+	5	2	6
2	3	7	1
1		1	

Continue to develop with addition of two four-digit numbers and with decimals (in the context of money or measures).

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Addition – Stage 6

• Add whole numbers with more than 4 digits, including using formal written method (column addition)

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to teach the use of **empty number lines** with larger numbers (and decimals), as appropriate.

Continue to develop the **formal written method** for addition with larger numbers (and decimal numbers) and with the addition of three or more numbers:

21848 + 1523 = 23371

Continue to use the language of place value to ensure understanding. Ensure that the digits that have been 'carried' are recorded under the line in the correct column.

Use the **formal written method** for the addition of decimal numbers:

 $\pounds154.75 + \pounds233.82 = \pounds388.57$

 $\begin{array}{r}
 154.75 \\
 + 233.82 \\
 \underline{388.57} \\
 1
 \end{array}$

Continue to use the language of place value to ensure understanding.

Ensure that the decimal points line up.

Continue to practise and apply the formal written method throughout stage 6.

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Addition – Stage 7

Children will continue to practise and use the formal written method for larger numbers and decimals and use these methods when solving problems, when appropriate (see previous stage's guidance for methods).

Our aim is that by the end of Y6, children use mental methods (with jottings) when appropriate, but for calculations that they cannot do in their heads, they use an efficient formal written method accurately and with confidence.

Stages in Subtraction

Subtraction – Stage 1

Children will engage in a variety of counting songs and rhymes and practical activities.

In practical activities and through discussion they will begin to use the vocabulary associated with subtraction.

They will find one less than a given number.

They will begin to relate subtraction to 'taking away' using objects to count 'how many are left' after some have been taken away.

$$6 - 2 = 4$$

'Take two apples away. How many are left?'

Children will begin to count back from a given number.

Subtraction – Stage 2

- Given a number, identify one less
- Read, write and interpret mathematical statements involving subtraction (-) and the equals (=) sign
- Subtract one- digit and two-digit numbers within 20, including zero
- Solve missing number problems eg 20 = 15

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Children will continue to practise counting back from a given number.

Initially use a number track to count back for subtraction:

Initially use a number track to count on for addition, counting on from the largest number:



9 - 5 = 4

'Put your finger on number nine. Count back 5.'





11 - 9 = 2



The difference between nine and eleven is two.

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Subtraction – Stage 3

31

36

Subtract numbers using concrete objects, pictorial representations, and mentally, including:

- A two digit number and ones
- A two digit number and tens
- Two two-digit numbers

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Counting back using an empty number line within 100, in ones...



76

Use in conjunction with a 100 square to show jumps of tens and ones/units.

Counting on to find a small difference

Introduce complementary addition to find differences (only use for small differences). The use of models is extremely important here to understand the idea of "difference" (see stage 2 guidance).

Count up from the smallest number to the largest to find the difference.



Subtraction – Stage 4

• Subtract numbers with up to three digits, using formal written method of column subtraction

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Further develop the use of the empty number line with calculations that bridge 100:



Use practical equipment to support counting back in tens and bridging 100 such as 200 grid, Numicon, Cuisinaire rods etc.



Extend with larger numbers by counting back...

216 - 27 = 189



...and by counting on to find the difference (small difference):

$$231 - 198 = 33$$



Subtraction – Stage 5

Introduce the **expanded written method** with the calculation presented both horizontally and vertically (in columns) and **supported with practical activities**. Use two-digit numbers when introducing this method, initially:

$$78 - 23 = 55$$
70 and 8
 $-20 \text{ and } 3$
 $50 \text{ and } 5 = 55$ 'Partition numbers into tens and ones. Subtract
the ones, and then subtract the tens. Recombine to
give answer.'
Use practical activities (such as Dienes) to support the teaching
of this method.

NB In this example decomposition (exchange) is not required.

You may replace the 'and' with a + symbol or give the place value column headings to avoid confusion.

This will lead into the formal written method:

78	Use the language of place value to ensure understanding.
<u>-23</u>	'Eight subtract three, seventy subtract twenty.'
<u>55</u>	

NB A number line would be an appropriate method for this calculation but use two digit numbers to illustrate the formal written method initially.

Introduce the expanded written method where exchange/decomposition is required:

73 - 27 = 46

70 + 3	becomes	60 and13
- 20 + 7		<u>- 20 and 7</u>
		40 + 6 = 46

73 is partitioned into 60 and 13 in order to calculate 73 - 27

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This can be demonstrated practically and does not have to be recorded

NB children will need to practise partitioning numbers in this way. **Base- ten materials** could be used to support this (such as Dienes).

When **children are confident** with the expanded method introduce the **formal written method**, involving **decomposition/exchange**:

73 - 27 = 46	
$ \begin{array}{r} 6 & 13 \\ 7 & 3 \\ \bullet & 2 & 7 \\ 4 & 6 \end{array} $	Use the language of place value to ensure understanding. 'We can't subtract seven from 3, so we need to exchange a ten for ten ones to give us 60 and 13.
<u> </u>	Use base ten / Dienes materials to support understanding

If children are confident, extend the use of the formal written method with numbers over 100, returning to the expanded method first, if necessary.

235 - 127 = 108

2 15	Use the language of place value to ensure understanding.
2 3 5	In this example, it has only been necessary to exchange from
· 1 2 7	the tens column.
108	

Use **base ten / Dienes** materials to support understanding

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Subtraction – Stage 5 – More complex methods

• Subtract numbers with up to 4 digits using the formal written method of columnar subtraction where appropriate

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to teach the use of **empty number lines** with three and four digit numbers, as appropriate.

Continue to develop the **formal written method of subtraction** by revisiting the expanded method first, if necessary. Continue to use base -ten / Dienes materials to support understanding.

258 - 73 = 185

200	and	50	and	8		100	and	150	and	8
	•	70	and	3	becomes	-		70	and	3
						100	and	80	and	<u>5 </u> = 185

This can be demonstrated practically and does not have to be recorded

This leads to the **formal written method**, involving decomposition...

1	15		
2	5	8	Use the language of place value to ensure understanding
-	7	3	In this example, it has been necessary to exchange from
1	7	5	the hundreds column.

Further develop by subtracting a three-digit number from a three-digit number:

637 - 252 = 385

600 ((and) 30	(and)	7	500	(and)	130	(and)	7	
-200 ((and) 50	(and)	2	-200	(and)	50	(and)	2	
				<u>300</u>	(and)	80	(and)	5	= 385

Ensure that children are confident in partitioning numbers this way.

This leads to a formal written method:

5	13	
6	3	7
-2	5	2
3	8	5

Use the language of place value to ensure understanding and use base-ten / Dienes materials, if necessary.

When **children are confident**, develop with four-digit numbers and decimal numbers (in context of money and measures).

3625 - 1219 = 2406

		1	15
3	6	2	5
-1	2	1	9
2	4	0	6

NB. If, at any time, children are making significant errors, return to the previous stage in calculation.

Subtraction – Stage 6

• Subtract whole numbers with more than 4 digits, including using formal written method (column subtraction)

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to teach the use of **empty number lines** with larger numbers and decimals, as appropriate.

Continue to develop the formal written method for subtraction with three and four digit numbers (see stage 5 guidance), returning to an expanded method and using base Ten / Dienes materials, if necessary.

503 - 278 = 225

500	0	3	400	90	13	In this example 503 has to be
<u>- 200</u>	70	8	<u>- 200</u>	70	8	partitioned into 400 + 90 + 13
			<u>200</u>	20	5	in order to carry out the
						Subtraction calculation.

This leads to the **formal written method** (there is potential for error in this example):

4	9	13	
5	0	3	There are no tens in the first number (503) so we have to
-2	7	8	exchange a hundred for 10 tens before we can exchange
2	2	5	a ten for 10 ones/units.

NB It would be appropriate to discuss the use of mental calculation methods with an example like this one, i.e. would an empty number line be a more efficient method for these numbers?

When children are confident extend with larger numbers (and decimal numbers). Return to an expanded method, if necessary.

12731 - 1367 = 11364

 $\begin{array}{r}
1 & 2 & \overline{7 \cdot 3 \cdot 1} \\
 -1 & 3 & 6 & 7 \\
 column. & \underline{1 \cdot 13 \cdot 6 \cdot 4}
\end{array}$

In this example it has been necessary to exchange from the tens and the hundreds

NB If children are making significant errors, provide calculations where only one exchange is required.

Introduce subtraction of decimals, initially in the context of money and measures.

£166.25 – £83.72 = £82.53 ¹⁶⁵ ¹² 1 6 6. 2-5 <u>-8 3 . 7 2</u> <u>8 2 . 5 3</u> Ensure the decimal point lines up.

Continue to practise and apply the formal written method with large numbers and decimals throughout year five.

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Subtraction – Stage 7

No objectives have been included in the programmes of study explicitly related to written methods for subtraction in Y6. However, there is an expectation that children will continue to practice and use the formal written method for larger numbers and decimals and use these methods when solving problems, when appropriate (see previous stage' guidance for methods).

Our aim is that by the end of Y6 children use mental methods (with jottings) when appropriate, but for calculations that they cannot do in their heads, they use an efficient formal written method accurately and with confidence.

Stages in Multiplication

Multiplication – Stage 1

Children will engage in a wide variety of songs and rhymes, games and activities. In practical activities and through discussion they will begin to solve problems involving doubling.





'Three apples for you and three apples for me. How many apples altogether?'

Multiplication – Stage 2

- Solve one-step problems involving multiplication by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher
- Count in multiples of twos, fives and tens (to the 10th multiple)

Children will count repeated groups of the same size in practical contexts. They will use the vocabulary associated with multiplication in practical contexts. They will solve **practical problems** that involve combining groups of 2, 5 or 10. E.g. socks, fingers and cubes



'Six pairs of socks. How many socks altogether? 2, 4, 6, 8, 10, 12'



'Three pots of ten crayons. How many crayons altogether? 10, 20, 30'





'Five groups of two faces. How many faces altogether? 2, 4, 6, 8, 10' Two groups of five faces. How many faces altogether? 5, 10'



Continue to solve problems in practical contexts and develop the language of early multiplication, with appropriate resources, throughout stage 2.

Multiplication – Stage 3

- Recall and use multiplication facts for the 2, 5 and 10 multiplication tables
- Calculate mathematical statements for multiplication within the multiplication tables and write them using the multiplication (x) and equals (=) signs
- solve problems involving multiplication, using materials, arrays, repeated addition, mental methods, and multiplication facts, including problems in contexts
- show that multiplication of two numbers can be done in any order (commutative)

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Children will use a range of vocabulary to describe multiplication and use practical resources, pictures, diagrams and the x sign to record.

Combining Groups (repeated addition):



'3 groups of 10 crayons'
'How many crayons altogether?'
'10 + 10 + 10 = 30'
'3 groups pf 10' ' 3 times 10'
'3 x 10 = 30' '10 x 3 = 30'



'5 groups of 3' '5 lots of 3' '3 + 3 + 3 + 3 + 3 = 15'

'5 times 3' '3 multiplied by 5' '5 x 3 = 15' '3 x 5 = 15'

Use arrays to support multiplication

 $6 \times 5 = 30$

'5 + 5 + 5 + 5 + 5 + 5 = 30'

'6 rows of 5'

'6 groups of 5'

'5 groups of 6'

'5 x 6 = 30'

'6 x 5 = 30'





Make the link to repeated addition.

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Multiplication - Stage 4

- Recall and use multiplication facts for the 3, 4 and 8 multiplication tables (continue to practise the 2, 5 and 10 multiplication tables)
- Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to a formal written method

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to use number lines and arrays to support multiplication, as appropriate (see stage 3 guidance).



Partitioning method for multiplication of a teen number by a one-digit number:

 $13 \times 5 = 65$ (Partition 13 into 10 + 3)

 $10 \times 5 = 50$ $3 \times 5 = 15$

50 + 15 = 65

Demonstrate the partitioning method using **a number line**:



Grid Method (teen number multiplied by a one- digit number):

13 x 8 = 104

X	10	3
8	80	24

'Partition 13 into 10 + 3 then multiply each number by 8. Add the partial products (80 and 24) together.'

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Multiplication- Stage 5

- Recall multiplication facts for multiplication tables up to 12 × 12
- Multiply two-digit and three-digit numbers by a one-digit number using formal written layout

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to use empty number lines, as appropriate (see stage 4 guidance).

Further develop the grid method for two-digit numbers multiplied by a one- digit number.

36 x 4 = 144

Х	30	6
4	120	24

120 + 24 = 144 (add the partial products)

Expanded short multiplication (two-digit number by a one-digit number):

 $36 \times 4 = 144$ $30 \quad 6$ $\times \quad 4$ $24 \quad (4 \times 6 = 24)$ $+ 120 \quad (4 \times 30 = 120)$ - 144

Include an addition symbol when adding partial products.

Refine the recording in preparation for the formal short multiplication

36 x	4 = 144
36	
<u>x 4</u>	
24	(4 x 6)
120	(4 x 30)
<u>144</u>	
	36 <u>x4</u> 24 <u>120</u>

This leads to **short multiplication (formal method)** of a two–digit number multiplied by a onedigit number:

36 x 4 = 144	
36 <u>X4</u>	Use the language of place value to ensure understanding
<u>144</u> 2	Ensure that the digit 'carried over' is written under the line in the correct column.

Continue to practise the formal method of short multiplication of a two-digit number by a one -digit number throughout stage 5

If children are confident, continue to develop short multiplication with three- digit numbers multiplied by a one-digit number.

If necessary, return to the grid method and/or expanded method first:

127 x 6 = 762

Х	100	20	7
6	600	120	42

600 + 120 + 42 = 762 (add the partial products)

This leads to **expanded short multiplication**:

127 x 6 = 762

1 X	2	7 6	
<u>//</u>	4	2	(6 x 7)
+ 1	2	0	(6 x 20)
+ 6	0	0	(6 x 100)
7	6	2	. ,

This will lead into short multiplication (formal method):



Use the language of place value to ensure understanding

Ensure that the digits 'carried over' are written under the line in the correct column.

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Multiplication – Stage 6

• Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Build on the work covered in stage 5 with the **formal method of short multiplication** (two-digit number multiplied by a one-digit number).

When children are confident introduce multiplication by a two-digit number. If necessary, return to the grid method and/or expanded method first.

Grid method (two-digit number multiplied by a teen- number):

23 x 13 = (20 + 3) x (10 + 3) = 299

Х	20	3
10	200	30
3	60	9

Add the partial products (200+30) + (60+9) = 299

+ 69 299

230

Expanded long multiplication (two-digit numbers multiplied by a teen-number)

23 x 13 = 299

2 3	
<u>X13</u>	
9	(3 x 3)
60	(3 x 20)
+ 3 0	(10 x 3)
<u>200</u>	(10 x 20)
299	

This leads into ...

Compact long multiplication (formal method):

23 x 13 = 299

23		Use the language of place value to ensure understanding
<u>X13</u>		
+ 6 9	(3 x 23)	
<u>230</u>	(10 x 23)	Add the partial products
<u>299</u>		

Extend to larger two-digit numbers (returning to the grid method and then expanded method if necessary)

When children are confident with long multiplication extend with three-digit numbers multiplied by a two-digit number, returning to the grid method first, if necessary:

124 x 26 = 3	224	
124 <u>X26</u>		Use the language of place value to ensure understanding
+7 4 $424 8 03 2 2 4$	(6 x 124) (20 x 124)	Add the partial products
1 1		The prompts (in brackets) can be omitted if children no longer need them.

Extend with short and long multiplication of decimal numbers (initially in the context of money and measures), returning to an expanded method first, if necessary (see stage 7guidance).

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Multiplication – Stage 7

• Multiply multi-digit numbers (including decimals) up to 4 digits by a two-digit whole numbers using the formal written method of multiplication

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to practise and develop the **formal short multiplication** method and **formal long multiplication** method with larger numbers and decimals throughout Y6. Return to an expanded forms of calculation initially, if necessary (see stage 6 guidance).

The grid method (decimal number multiplied by a two-digit number):

53.2 x 24 = 1276.8

Х	50	3	0.2	
20	1000	60	4	1064.0
4	200	12	0.8	212.8
				1276.8

The formal written method of long multiplication:



It is an option to include .0 in this example, but not

essential.

The prompts (in brackets) can be omitted if children no longer need them.

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NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Our aim is that by the end of stage 7 children use mental methods (with jottings) when appropriate, but for calculations that they cannot do in their heads, they use an efficient formal written method accurately and with confidence.

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Stages in Division

Division – Stage 1

Children will engage in a wide variety of songs and rhymes, games and activities. In practical activities and through discussion they will begin to solve problems involving halving and sharing.





Share the apples between two people.

'Half of the apples for you and half of the apples for me.'

Division – Stage 2

- Solve one-step problems involving division by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher
- Count in multiples of twos, fives and tens (to the 10th multiple)

Children will start with practical sharing using a variety of resources. They will share objects into equal groups in a variety of situations. They will begin to use the vocabulary associated with division in practical contexts.

'Share these eight apples equally between two children. How many apples will each child have?'







'Share 20 crayons between 2 pots.' 'How many crayons are in each pot?' Children will move from **sharing** to **grouping** in a practical way



'Put 20 crayons into groups of 10. How many pots do we need?'

Use arrays to support early division



'How many faces altogether? How many groups of two?'



'Five groups of two.'



'How many groups of 5?'

'10 shared equally between 2 people.'

'Half of ten is five.'

Continue to solve problems in practical contexts throughout stage 2, and develop the language of early division, with appropriate resources.

Division – Stage 3

- Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables
- Calculate mathematical statements for division within the multiplication tables they know and write them using the division (÷) and equals (=) signs
- Solve problems involving division, using materials, arrays, repeated subtraction, mental methods, and multiplication and division facts, including problems in contexts

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Children will use a range of vocabulary to describe division and use practical resources, pictures, diagrams and the ÷sign to record, using multiples that they know.

Sharing and grouping:



'30 crayons shared equally between 3 pots.' (Sharing) 'We have 30 crayons and put ten in each pot. How many pots do we need?' (Grouping).

 $30 \div 10 = 3$ $30 \div 3 = 10$



'How many groups if 5?'

'30 divided by 10 = 3'

'30 divided by 3 = 10'

'15 shared equally between 3 people is...?'

'15 divided by 3 equals 5'

'15 divided by 5 equals 3'

 $15 \div 5 = 3$ $15 \div 3 = 5$





How many groups of 3?

How many groups of 5?

15 shared between 3 people is...?

15 shared between 5 people is...?

15 divided by 5 = 315 divided by 3 = 5

When children are ready, use an empty number line to count forwards:



'How many jumps of 5 make 30?'



NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Division – Stage 4

- Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables (continue to practise the 2, 5 and 10 multiplication tables)
- Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers divided by one-digit numbers, using mental and progressing to a formal written method

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to use practical resources, pictures, diagrams, number lines, arrays and the ÷ sign to record, using multiples that they know, as appropriate (see stage 3 guidance).

Using an empty number line to count forwards...

$24 \div 3 = 8$

'How many threes are in 24?'



'How many groups of three in 24?'

NB If, at any time, children are making significant errors, return to the previous stage in calculation

Division – Stage 5

- Recall multiplication and division facts for multiplication tables up to 12 × 12
- Use place value, known and derived facts to divide mentally
- Divide two-digit and three-digit numbers by a one-digit number using formal written layout (not explicitly stated in the programmes of study but implied in the non-statutory guidance)

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to write and calculate mathematical statements for division using the multiplication tables that the children know e.g.



8 r1

3 25

NB Remainders are not specifically referred to until year 5 in the National Curriculum. However, this may be an appropriate point to introduce them using familiar multiplication facts.

This could be modelled using an empty number line, <u>if necessary</u>: **Division using partitioning** (two digits divided by one digit):

65 = 50 + 15 Partition 65 into 50 and 15 $50 \div 5 = 10$ $15 \div 5 = 3$ 10 + 3 = 13

NB Children will need to practise partitioning in a variety of ways.

98 ÷ 7 = 14

98 = 70 + 28 Partition 98 into 70 and 28 $70 \div 7 = 10$ $28 \div 7 = 4$ 10 + 4 = 14

This could be modelled on an empty number line to further develop understanding.

NB Children will need to practise partitioning in a variety of ways.

Chunking Method

```
73 ÷ 5 How many 5s make 73?
```

```
73
- <u>50</u> (10x5)
23
- <u>20</u> (4x5)
3
```

How many 5s have been subtracted? 14 sets of 5, with 3 left over

73 ÷ 5 = 14 r 3

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Division – Stage 6

• Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Continue to practise the formal written method of short division with whole number answers...

184
$$\div$$
 8 = 2382381 8 24Make the link between the partitioning method (see stage 5 guidance)

...and with remainders:

432 ÷ 5 = 86 r2

The remainder can also be expressed as a fraction, 2/5 (the remainder divided by the divisor): $432 \div 5 = 86 2/5$

Continue to practise, develop and extend the formal method of short division, with and without remainders. Interpret and express remainders according to the context.

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Division – Stage 7

- Divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context
- Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context

NB Ensure that children are confident with the methods outlined in the previous stage's guidance before moving on.

Dividing by a two-digit number using a formal method of long division:

Standard short division does not help with the following calculation. However, it can be solved using **long division** (by repeated subtraction using multiples of the divisor):

144÷16 = 9

	9	
16	144	Multiples of the divisor (16) have been subtracted from
	<u>- 6 4</u> (4 x 16)	the dividend (144)
	80	
	<u>-64</u>	'4 (lots of 16) + 4 (lots of 16) + 1 (lot of 16) =
	16	9 (lots of 16)'
	<u>-16</u>	
	0	There is no remainder
	0	

Practise the formal method of short division, with and without remainders, using the language of place value to ensure understanding (see stage 6guidance).

496 ÷ 11 = 45 r1

The remainder can also be expressed as a fraction, 1/11 (the remainder divided by the divisor)

This is an alternative way of recording formal long division:

43215 = 28.8

28.8	
15 432.0	NB Only teach this method when children are
<u>300</u>	completely secure with the previous method.
132	
<u>120</u>	The remainder is expressed as a decimal.
120	
<u>120</u>	
0	

NB If, at any time, children are making significant errors, return to the previous stage in calculation.

Our aim is that by the end of Y6 children use mental methods (with jottings) when appropriate, but for calculations that they cannot do in their heads, they use an **efficient formal written method** accurately and with confidence.

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